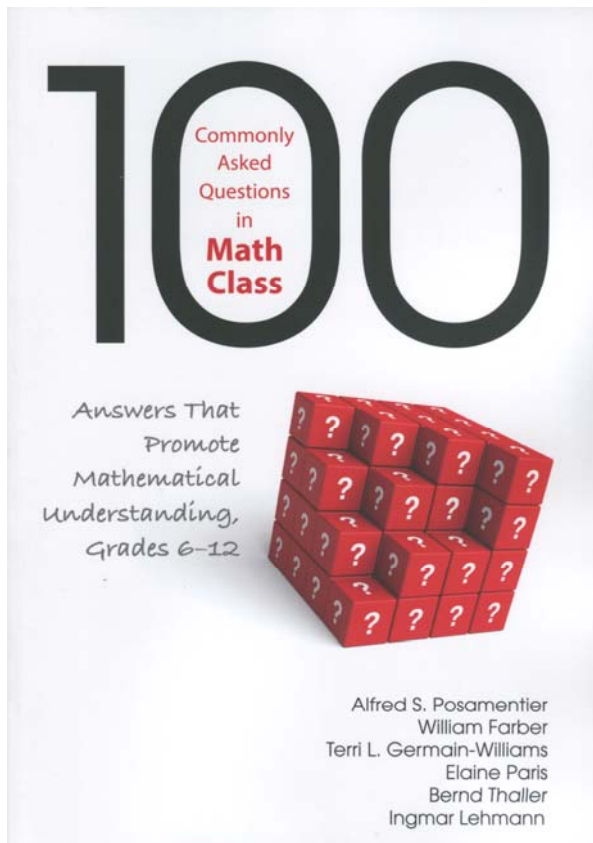


Errata and more:



100 Commonly Asked Questions in Math Class. Answers That Promote Mathematical Understanding, Grades 6-12.

Alfred S. Posamentier, William Farber,
Terri L. Germain-Williams, Elaine Paris,
Bernd Thaller, Ingmar Lehmann

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Errata

We appreciate any comments about the book as well as any typographical errors that have not yet been detected so that they can be incorporated in future printings of the book.

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